Using networks to measure similarity between genes: association index selection

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Biological networks can be used to functionally annotate genes on the basis of interactionprofile similarities. Metrics known as association indices can be used to quantify interaction-profile similarity. We provide an overview of commonly used association indices, including the Jaccard index and the Pearson correlation coefficient, and compare their performance in different types of analyses of biological networks. We introduce the Guide for Association Index for Networks (GAIN), a web tool for calculating and comparing interaction-profile similarities and defining modules of genes with similar profiles.

Biological processes are orchestrated through complex interaction networks. Networks are modeled as graphs that depict interactions ('edges') between biological entities such as genes, tissues, proteins and metabolites ('nodes'; see **Box 1**). If only one type of node is involved, as in protein-protein^{1,2} or genetic interaction networks³, the graph is defined as monopartite. Bipartite graphs, by contrast, describe interactions between two different types of nodes (X-type and Y-type), with edges connecting only nodes of different types (Fig. 1a). Bipartite graphs include protein-DNA interaction networks^{4–6}, metabolic networks^{7,8}, phenotypic networks⁹ and expression networks^{10–14}.

Networks are powerful tools for gene function annotation. For instance, the 'guilt-by-association' principle postulates that if a node with an unknown function has an interaction profile similar to that of a node with a known function, its function may be similar as well^{2,15}. Additionally, network analysis can identify modules—neighborhoods comprising nodes with similar interaction profiles that can point to functional relationships between larger sets of genes^{16,17}. Although seemingly intuitive, it is

not trivial to know how to best capture interactionprofile similarity between nodes, as numerous metrics, or association indices, can be used, and because each index can provide different values and rank similarity between pairs of nodes in a different order. Here, we provide an overview of commonly used association indices. We discuss the differences and similarities between association indices and provide a set of guidelines and a web tool for their selection for different applications.

Types of association indices

We focus here on bipartite networks that connect X-type nodes to Y-type nodes (Fig. 1a). In these networks, association indices can be used to measure shared Y-type nodes between two X-type nodes, or vice versa. An association index can measure interactionprofile similarity between X-type nodes A and B by calculating the shared partners ($|N(A) \cap N(B)|$), in relation to their total number of interactions ('node degree'), defined as |N(A)| and |N(B)|, and the total number of Y-type nodes in the network (n_v) (**Fig. 1a**). There are three main types of indices, each of which uses the variables mentioned above in a different way (see Box 2).

Similarity indices reflect the proportion of overlap and consider only the number of shared interactions between two X-type nodes and the individual degrees of these nodes, but they do not take the total number of Y-type nodes in the network into account. There are many similarity indices, most of which scale interaction-profile similarity between 0 and 1 (ref. 18) (Supplementary Table 1). We will focus on four that are commonly used in genomics and systems biology (see Box 2). The Jaccard index calculates the proportion of Y-type nodes shared between two X-type

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BOX 1 GLOSSARY OF TERMS

A **graph** is a pair G = (N, E) comprising a set N of nodes connected by a set E of edges.

The degree of a node A (|N(A)|) is defined as the number of nodes with which it interacts.

Hubs are nodes with a disproportionately high degree.

A module is a set of highly interconnected nodes.

A monopartite graph contains only one type of node.

A bipartite graph contains two types of nodes (X-type and Y-type nodes), and connections occur only between nodes of a different type.

An **association index** is a measure that quantifies interaction-profile similarity.

An **association network** is a network in which two nodes of the same type (for example, only X-type nodes) are connected by an edge if their similarity exceeds a selected threshold.

nodes relative to the total number of Y-type nodes connected to either X-type node. The Simpson index (equal to the meet/min index¹⁹ and similar to the topological overlap coefficient¹⁶) considers the number of shared Y-type nodes relative to the smallest degree of either X-type node. The geometric index calculates the square of the number of shared interactions between two X-type nodes, divided by the product of their individual degrees. Finally, the cosine index corresponds to the square root of the geometric index.

Unlike similarity indices, matching indices, such as the simple matching coefficient and the Hamann index (**Supplementary Table 1**), consider the proportion of shared Y-type nodes as well as Y-type nodes that are not connected to either of the two X-type nodes. Because biological networks are sparse, shared nonpartners can contribute more to the similarity between two nodes than shared partners. Therefore, matching indices are not appropriate for the analysis of most biological networks and will not be discussed further.

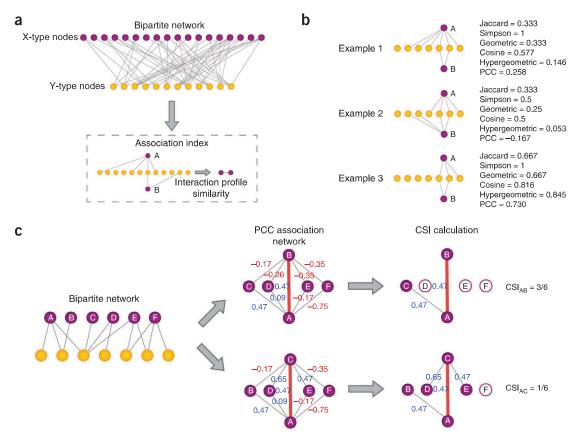


Figure 1 | Measuring interaction-profile similarity between two nodes using association indices. (a) Bipartite graphs connect two types of nodes: X-type (purple) and Y-type (yellow). The interaction-profile similarity between a pair of X-type nodes (A and B) is determined on the basis of the number of shared Y-type nodes, the total number of Y-type nodes connected to A and B, and the total number of Y-type nodes in the network. (b) Association index comparison. For each pair of X-type nodes, the Jaccard, Simpson, geometric, cosine and hypergeometric indices and PCC were calculated on the basis of their interactions with Y-type nodes. (c) CSI calculation between nodes A and B for a bipartite network involving six X-type nodes (purple) and seven Y-type nodes (yellow). For each pair of X-type nodes the PCC was calculated (blue, positive values; red, negative values). In the PCC association network all the edges connected to A or B are highlighted. CSI_{AB} represents the fraction of X-type nodes connected to both A and B, with PCC < PCC_{AB} – 0.05. The CSI was also calculated between A and C.

BOX 2 DEFINITIONS OF ASSOCIATION INDICES

The Jaccard index is the proportion of shared nodes between A and B relative to the total number of nodes connected to A or B.

$$J_{AB} = \frac{|N(A) \cap N(B)|}{|N(A) \cup N(B)|}$$

The **Simpson** index is the proportion of shared nodes relative to the degree of the least-connected node.

$$S_{AB} = \frac{|N(A) \cap N(B)|}{\min(|N(A)|, |N(B)|)}$$

The geometric index corresponds to the product of the proportion of shared nodes between A and B.

$$G_{AB} = \frac{|N(A) \cap N(B)|^2}{|N(A)| \cdot |N(B)|}$$

The cosine index is the geometric mean of the proportions of shared nodes between A and B.

$$C_{AB} = \frac{|N(A) \cap N(B)|}{\sqrt{|N(A)| \cdot |N(B)|}}$$

The Pearson correlation coefficient is the correlation between the interaction profiles of A and B.

$$\mathsf{PCC}_{\mathsf{AB}} = \frac{\mid \textit{N}(\mathsf{A}) \cap \textit{N}(\mathsf{B}) \mid . \; \mathsf{n}_{\mathsf{y}} - \mid \textit{N}(\mathsf{A}) \mid . \mid \textit{N}(\mathsf{B}) \mid}{\sqrt{\mid \textit{N}(\mathsf{A}) \mid . \mid \textit{N}(\mathsf{B}) \mid . \; (\mathsf{n}_{\mathsf{y}} - \mid \textit{N}(\mathsf{A}) \mid) . \; (\mathsf{n}_{\mathsf{y}} - \mid \textit{N}(\mathsf{B}) \mid)}}$$

The **hypergeometric** index is the log-transformed probability of having an equal or greater interaction overlap than the one observed between A and B.

$$\mathsf{H}_{\mathsf{AB}} = -\log \sum_{i = |N(\mathsf{A}) \cap N(\mathsf{B})|}^{\min(|N(\mathsf{A}), N(\mathsf{B})|)} \frac{\binom{|N(\mathsf{A})|}{i} \cdot \binom{\mathsf{n}_{\mathsf{y}} - |N(\mathsf{A})|}{|N(\mathsf{B})| - i}}{\binom{\mathsf{n}_{\mathsf{y}}}{|N(\mathsf{B})|}}$$

The connection specificity index (CSI) is defined as the fraction of X-type nodes that have an interaction profile similarity with A and B that is lower than the interaction profile similarity between A and B itself.

$$\begin{aligned} \text{CSI}_{AB} &= 1 - \frac{\# nodes \, connected \, to \, A \, \, or \, B \, \, with \, PCC \geq PCC_{AB} - 0.05}{n_y} \\ &= \frac{\# nodes \, connected \, to \, A \, \, and \, B \, \, with \, PCC < PCC_{AB} - 0.05}{n_y} \end{aligned}$$

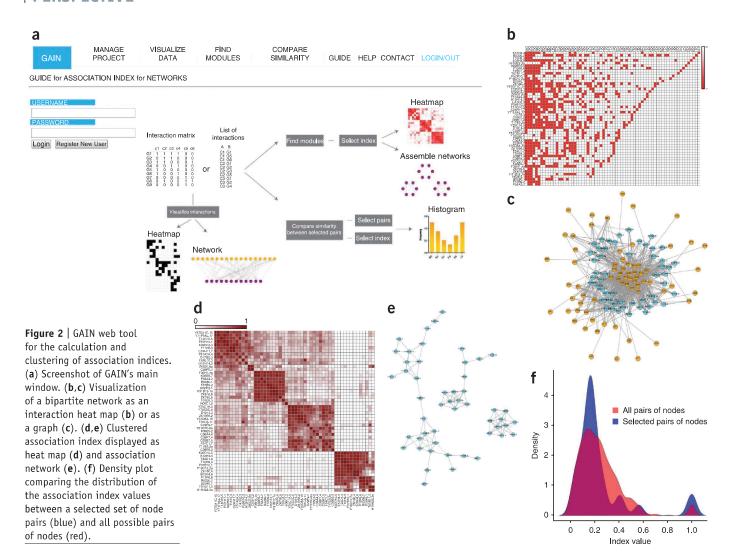
Statistic-based indices employ probability distributions (such as chi-square and Fisher's exact test) to determine the likelihood of observing a certain overlap between the interaction profiles of two X-type nodes given their degree and the total number of Y-type nodes in the network ¹⁸ (**Supplementary Table 1**). We will discuss two of the most commonly used statistic-based indices.

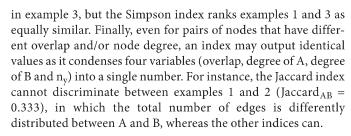
The Pearson correlation coefficient (PCC) was originally developed to measure the linear relationship between two continuous variables, such as protein and mRNA levels. This metric can also be applied to bipartite networks where interactions are either present or absent. The PCC provides a value between -1 and 1 that describes how well the interactions overlap. A PCC of 1 indicates a perfect overlap, 0 corresponds to the number of shared interactions expected by chance and -1 depicts perfect anticorrelation. The hypergeometric index calculates the log-transformed

probability of observing an equal or greater number of shared nodes by chance and, therefore, measures the significance rather than the magnitude of the overlap.

Comparing association indices

Different association indices can provide different values of interaction-profile similarity. We illustrate this using three small example networks in which two X-type nodes, A and B, share different numbers of Y-type nodes, out of a total of seven (**Fig. 1b**). In each example, different indices can provide different values, ranging from perfect similarity (Simpson_{AB} = 1 in example 1) to low similarity (hypergeometric_{AB} = 0.146 in example 1). Further, different indices can rank the interaction-profile similarity between a pair of nodes in different orders. For instance, according to most indices the profiles of A and B are most similar





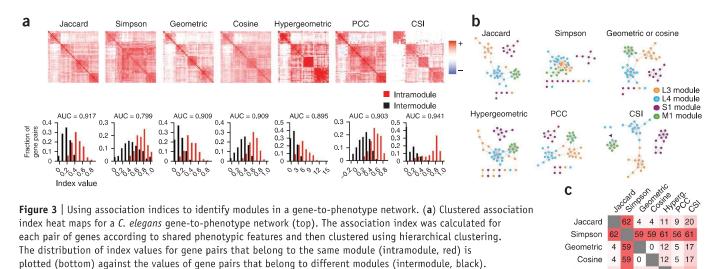
Nonspecific interactions can drive similarity

The indices mentioned above consider the similarity in interacting partners between two X-type nodes but not the interaction specificity. Two issues need to be considered. First, Y-type hubs may confer artificially high levels of interaction-profile similarity: if half of all X-type nodes bind a Y-type hub, this overlap is not very informative. Second, not all Y-type nodes are independent, which may also confer exaggerated levels of interaction-profile similarity. For instance, neurons can be classified into different categories on the basis of the tissues in which they are located. Different types of neurons express common genes. Thus, in a gene-to-tissue network where genes are connected to the tissues in which they are expressed, neuronal genes may be connected to many classes of neurons, artificially increasing their similarity.

The connection specificity index (CSI) provides a contextdependent measure that mitigates the effect of nonspecific interactions by ranking the significance of similarity between two X-type nodes according to the specificity of their shared interaction partners⁹. The CSI between two nodes A and B is defined as the fraction of X-type nodes that have an interaction-profile similarity with A and B that is lower than the interaction-profile similarity between A and B themselves (see Box 2). As originally defined, the CSI employs the PCC as a first-level association index to rank the similarity between nodes, and then uses a constant of 0.05 to define the lower boundary of interaction-profile similarity⁹. When the constant is increased, the CSI provides a more stringent measure. Other association indices may also be used for a first-level ranking of interaction-profile similarity. Figure 1c illustrates an example in which the CSI reduces the influence of hubs. In this network, A and B interact with three and one Y-type nodes, respectively, and share one Y-type node, resulting in a $PCC_{AB} = 0.47$ (**Fig. 1c**). A and C also share one interaction partner and therefore $PCC_{AC} = 0.47$ as well. However, many other X-type nodes interact with the Y-type node connected to both A and C, hence this shared interaction is less specific. Applying CSI to these networks alleviates this problem: when a constant of 0.05 is used, $CSI_{AB} = 0.5$, whereas $CSI_{AC} = 0.17$ (**Fig. 1c**).







The area under the receiver operating characteristic curve (AUC) measures the separation between the two distributions. (b) The association networks shown were assembled by linking genes that have a top 10% CSI 20 61 17 17 26 15 PCC CSI 20 PCC CS

GAIN: a web tool for association indices and clustering

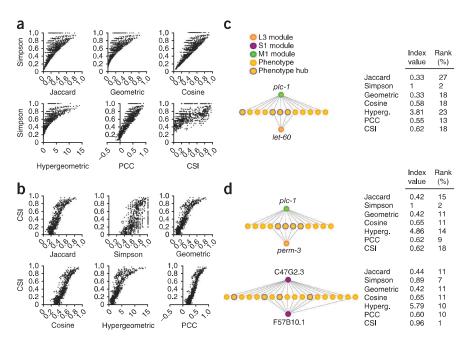
We developed GAIN (http://csbio.cs.umn.edu/similarity_index/login.php) (Fig. 2a and Supplementary Methods), which allows a user to upload an interaction data set and perform several tasks. First, interactions can be visualized as a heat map (Fig. 2b) or graph (Fig. 2c). Second, GAIN allows the user to find modules by calculating all pairwise values with a user-selected association index followed by hierarchical clustering and by displaying a heat map (Fig. 2d) or association network (Fig. 2e). Association networks contain one node type connected by an edge only when their interaction-profile similarity exceeds a user-selected threshold. Finally, GAIN can display a density plot to determine whether an association index can discriminate the interaction-profile similarity of a particular set of node pairs selected by the user from all node pairs (Fig. 2f). For instance, in a gene regulatory network

this can be used to determine whether pairs of highly homologous transcription factors have more similar interaction profiles than all possible pairs of transcription factors.

Figure 4 | Comparing association indices in the *C. elegans* gene-to-phenotype network. (a,b) Pairwise association index values for all genes according to shared phenotypic features for the Simpson index (a) and CSI (b), plotted against the values determined with the other indices. (c,d) The interaction-profile similarity between plc-1 and let-60 (belonging to different modules) (c), plc-1 and perm-3 (belonging to different modules) and between C47G2.3 and F57B10.1 (belonging to the same module) (d) were determined for all the association indices. The ranking of interaction-profile similarity across the entire network (in the top x% values from most to least similar) is indicated (right). Yellow nodes indicate phenotypes. Phenotype hubs (connected to more than 40% of the genes) are indicated with a blue outline. Hyperg., hypergeometric.

Finding network modules

Network modules are groups of nodes with relatively high interaction-profile similarity and can point to shared biological function between nodes. To compare how different association indices perform in the identification of network modules, we used two bipartite networks. The first is a subset of a *Caenorhabditis elegans* gene-to-phenotype network that connects 52 essential genes to 94 phenotypic features⁹. We used genes that belong to four modules manually determined by the authors of the original paper to benchmark the performance of the different indices. Association indices were calculated for each pair of genes according to their shared phenotypic features and then clustered into heat maps (**Fig. 3a**). Visual inspection shows that the Simpson index is least suitable for the identification of the four modules, and CSI performs the best. Consistent



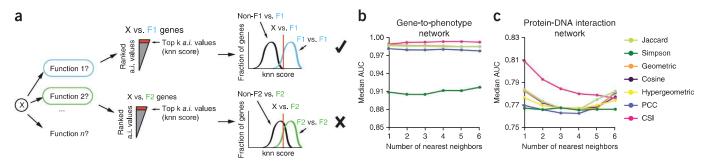
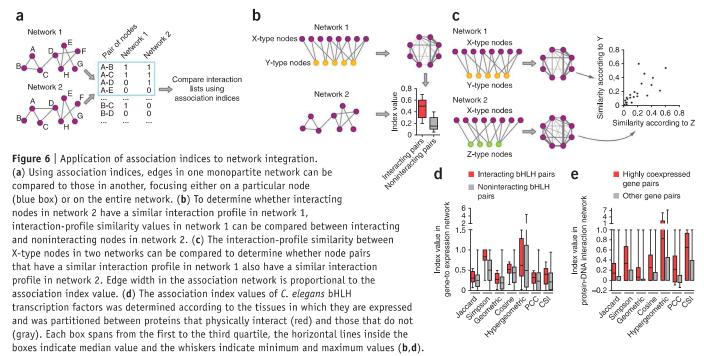


Figure 5 | Predicting gene function. (a) A k-nearest-neighbor (knn) algorithm was used to evaluate how well each index is able to assign genes to functional classes (F). To determine whether an uncharacterized gene X can be assigned a particular function, a knn score was determined as the average of the top k association index (a.i.) values between X and genes with that function. The knn values were then calculated for genes that have that function (blue and green) and for genes that do not (black curves). To assign a function to gene X, these values should be well separated (determined by calculating the AUC). a illustrates a case in which gene X can be assigned function 1 (F1, blue) but not function 2 (F2, green). The median AUC determined for all the functional classes was used as a measure of performance of the different association indices to predict gene function. (b) The median AUC calculated for the four functional classes in the C. elegans gene-to-phenotype network was determined for k values of 1 to 6 (number of nearest neighbors). (c) The median AUC calculated for the biological process GO slim terms in the yeast protein-DNA interaction network was determined for k values from 1 to 6.

with this observation, we found that CSI is best able to discriminate between the interaction-profile similarity between nodes that belong to the same module and that of nodes belonging to different modules (Fig. 3a).

Next, we asked which index performs best to delineate association networks for this gene-to-phenotype network. These networks connect nodes that have an interaction-profile similarity above a certain threshold. Therefore, they serve not only to delineate modules but also to identify nodes related to more than one module and nodes that are not related to any module. We used the top 10% of the values obtained with each index (Fig. 3b). CSI outperforms the other indices, as it (i) better demarcates the modules, (ii) leaves only two genes not assigned to any module and (iii) places only one gene into a module different from that

assigned by manual classification (Fig. 3b). Generally, association networks obtained with different indices exhibit a large degree of overlap in the edges included, except for those obtained with the Simpson index and CSI (Fig. 3c). Indeed, by determining all pairwise association index values for each pair of indices, i.e., by not limiting to the top 10%, comparisons involving Simpson or CSI were least correlated (Fig. 4a,b and Supplementary Fig. 1). This analysis of a real network further substantiates the notion that different indices can result in different values and ranking of interaction-profile similarity. Neither the Simpson index nor CSI is well correlated with any of the other indices, but the consequences in each case are quite different: for Simpson the poor correlation results in reduced module demarcation, whereas for CSI it results in precisely the opposite. The denominator in



(e) Association index values were determined for pairs of promoters in the yeast protein-DNA interaction network. The values for pairs of highly coexpressed genes (top 1%; red) and other gene pairs (bottom 99%; gray) are plotted.



Table 1 | Association index performance for different applications

	Jaccard	Simpson	Geometric	Cosine	Hypergeometric	PCC	CSI
Identifying network modules	**	*	**	**	**	**	***
Predicting gene function	**	*	**	**	**	**	***
Comparing two sets of node pairs ^a	**	***	**	**	*	***	*
Determining significance of overlap	No	No	No	No	Yes	No	No

Asterisks indicate qualitative strengths, with a greater number indicating greater utility. ^aAssessment depends on biological question or objective.

the Simpson index uses only the lower of the two overall node degrees, which can lead to artificially high levels of interactionprofile similarity, even for genes belonging to different modules (**Fig. 4c**). In the case of CSI, ranking similarity according to interaction specificity results in a higher value for gene pairs with shared specific phenotypes (C47G2.3 and F57B10.1), and a lower value for gene pairs with shared common phenotypes (plc-1 and *perm-3*) (**Fig. 4d**).

The second example network contains protein-DNA interactions between 102 yeast transcription factors and 542 promoters⁴. Association indices were calculated for each pair of promoters according to their shared transcription factors, and values were clustered into heat maps (Supplementary Fig. 2a). The heat maps are visually quite similar, and numerous modules can be detected. There were no previously benchmarked modules available. However, because genes with similar functions are frequently bound by the same transcription factor(s), we assessed the performance of the different indices by analyzing the biological process Gene Ontology (GO) enrichment in three different modules (Supplementary Fig. 2b). Two modules were detected equally well by all association indices (**Supplementary Fig. 2c**); however, for the third module significant enrichment (P < 0.001) for genes involved in the oxidation-reduction process was detected only by CSI and the Jaccard, geometric and hypergeometric indices (Supplementary Fig. 2c). Thus, association indices can perform differently in different types of networks and even within a network.

Predicting function of individual genes

Biologists frequently identify single genes of unknown functions, for instance in a genetic screen. So far, we have discussed network modules as a starting point for functional annotation. However, for analysis of only a single gene, there is no need to first comprehensively identify network modules. Moreover, modules are not always suitable for annotation of the function of every gene, as a gene may not belong to a clearly defined module and may have more than one function. An intuitive way to annotate gene function is to use the guilt-by-association principle, which postulates that two genes with similar functions have similar interaction profiles. One can assign functions to genes using a variety of different algorithms. Here, we use a k-nearest-neighbor algorithm that tests associations between genes and functions (Fig. 5a). An unknown gene can be assigned to each function F depending on (i) the top k association index values between that gene and the gene(s) that are known to have that function, and (ii) the specificity of the distribution of those values. In the example shown in **Figure 5a**, the highest score for the unknown gene (X) with genes with either known function 1 (F1, blue) or function 2 (F2, green) is similar (red lines). However, for function 1, the two distributions are largely separate, whereas for function 2 the two

distributions overlap greatly. Thus, function 1 can be assigned to gene X with greater confidence than function 2. We assessed which association index best predicts function using the two networks described above. Again, CSI was best able to assign genes to functional classes, and the Simpson index performed the worst (Fig. 5b,c). This result is consistent with the ability of CSI to consider interaction specificity.

Integrated networks

The integration of different types of networks enables the comparison of pairs of nodes across networks^{13,20}. Questions that can be answered include (i) whether directly interacting pairs of nodes in one network also tend to interact in another (Fig. 6a; note that this involves two monopartite networks), (ii) whether interacting nodes in one monopartite network have similar interaction profiles in a bipartite network (Fig. 6b) and (iii) whether pairs of nodes with similar interaction profiles in one bipartite network are also similar in another bipartite network (Fig. 6c). An example of the first type of question is whether the genes that encode physically interacting proteins also interact genetically. An example of the second type of question is whether proteins that physically interact tend to share phenotypes. Finally, an example of the third question is whether transcription factors that regulate a shared set of target genes are expressed in the same tissues and/or under the same conditions.

To determine whether interacting nodes in one monopartite network also interact in another network, the overlap between both sets of interactions can be determined, using association indices, on the basis of the number of shared edges between both networks, the number of edges in each network and the total number of node pairs (Fig. 6a). To determine the magnitude of similarity, Jaccard and Simpson are most suitable, and the hypergeometric index can be used to determine significance. The same approach can be used to compare interacting node pairs between modules in one network to those in another. Such 'cross-network module preservation' has been evaluated elsewhere²¹.

To integrate a monopartite and a bipartite (Fig. 6b), or two bipartite, networks (Fig. 6c), the biological question should inform index selection. We illustrate this with two data sets. The first is a multiparameter, integrated C. elegans basic helix-loophelix (bHLH) network comprising protein-protein interactions and gene-to-tissue expression patterns¹³. Each index revealed that interacting bHLH proteins are more often coexpressed than noninteracting ones (Fig. 6d). However, Simpson outperformed the other indices (Fig. 6d and Supplementary Fig. 3a). This is because a few bHLH proteins that bind many partners are broadly expressed, but each protein's partners are expressed in only a subset of tissues. This is best captured by the Simpson index, as it uses the minimum node degree in the denominator. The second data set is the yeast protein-DNA interaction network,

revealed that highly coexpressed genes have higher protein-DNA interaction-profile similarity than other gene pairs (Fig. 6e). The PCC best separated the two categories, and the Simpson index was least efficient (Supplementary Fig. 3b). The relatively poor performance of the Simpson index is because it considers the degree of only the least connected promoter. As a consequence, a promoter bound by many transcription factors may be regarded as similar to a promoter bound by few, some of which are shared. However, differences between transcription factors bound to promoters are also highly meaningful, as these may contribute to distinct gene-expression profiles. Conclusions

Different association indices can be used to compare interactionprofile similarity within and across networks, and different indices have strengths and weaknesses for different applications (Table 1). CSI is most suitable for predicting gene function and identifying modules. However, CSI levels the similarities between modules, which is a disadvantage in comparing modules. When the main goal is to compare the similarity between node pairs, the biological question should drive index selection. For instance, the Simpson index may be used to avoid penalizing large differences in node degree. If one wants, conversely, to capture this difference, other indices are more appropriate. The hypergeometric index should be used with caution to determine the magnitude of similarity between interaction profiles, as it does not scale linearly with the proportion of overlap. However, only this index is able to calculate the statistical significance of interactionprofile overlap.

integrated with a microarray coexpression network²². All indices

Note: Any Supplementary Information and Source Data files are available in the online version of the paper.

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AUTHOR CONTRIBUTIONS

J.I.F.B. and A.J.M.W. conceived the project; J.I.F.B. performed the data analysis with the assistance of A.D., J.N. and C.L.M.; A.D. and J.I.F.B. developed the GAIN web tool in collaboration with J.N., C.L.M. and J.M.S.; J.I.F.B. and A.J.M.W. wrote the paper.

COMPETING FINANCIAL INTERESTS

The authors declare no competing financial interests.

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